MUSHROOM SHAPED BUBBLES AND THE JET OF 1000 m/s

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ABSTRACT

The dynamics of a single, laser-induced cavitation bubble on top of a solid cylinder is studied both experimentally and numerically. When the bubble is generated close to the flat top along the axis of the cylinder and its maximum radius exceeds the one of the flat top surface, it collapses in the form of a mushroom with a footing on the cylinder, a long stem and a hat-like cap typical for a mushroom head. The head may collapse forming a thin, fast liquid jet into the stem, depending on bubble size and bubble distance to the top of the cylinder. The parameter space of initial distance to the cylinder, bubble size and cylinder radius is scanned numerically, partly compared to experiments and evaluated for the resulting jet velocity and jet length and other features. The results represent a contribution to understand the behavior of bubbles collapsing close to structured surfaces, in particular, how thin, fast jets are generated. An indication how the fast jet plays a role for erosion is given, as well.

Keywords: single cavitation bubble, CFD, high-speed imaging, laser-induced, rigid cylinder, fast jet

NOMENCLATURE

\[ D \ [m] \quad \text{distance bubble – object} \]
\[ R \ [m] \quad \text{bubble radius} \]
\[ p \ [Pa] \quad \text{pressure} \]
\[ U \ [m/s] \quad \text{velocity} \]
\[ \alpha \ [\text{-}] \quad \text{phase parameter} \]
\[ \lambda \ [m] \quad \text{wavelength} \]
\[ \mu \ [Pa \ s] \quad \text{viscosity} \]
\[ \rho \ [kg/m^3] \quad \text{density} \]

Subscripts and Superscripts

\[ \text{max} \quad \text{maximum} \]
\[ \text{eq} \quad \text{equivalent} \]
\[ \text{init} \quad \text{initial} \]
\[ * \quad \text{normalized quantity} \]
\[ n, \infty \quad \text{quantity at normal conditions} \]

1. INTRODUCTION

The phenomena described in this manuscript are explained in detail in [1]. This manuscript is to be understood as a summary of the main aspects from this publication, plus a small extension. For a full comprehension it is advisable to read the open access article [1] as well. The present manuscript is written with the assumption of familiarity of the reader with the single bubble cavitation phenomenon. If a text part in this manuscript is cited directly from [1] it is denoted by “([1])” at the end of the paragraph.

Despite considerable efforts to elucidate the erosion process by cavitation bubbles, the precise mechanisms are still under discussion. The dynamics of the bubble is highly influenced by many factors: The properties of the surrounding liquid (density, viscosity), the bubble contents (gas, vapour), the bubble-liquid interface (surface tension, coating), outer factors (pressure, temperature, gravity) and, in particular, the large class of geometrical constraints, i.e., boundaries or objects nearby with different properties from flat to curved or smooth to corrugated and solid to soft. For systematic studies on geometrical constraints, isolated single bubbles are required. The liquid breakdown induced by a focused laser light pulse has been used for this purpose ([1]).

In the past, investigation of bubble dynamics near structured objects got less attention than studies on flat or smooth surfaces. However, it is known that cavitation bubbles can reach, clean and also damage crevices, holes, trenches and other complicated surface features (see, e.g., [2]). Up to now, owing to the large variety of structures and constraints, only a few cases were already investigated for single bubble dynamics. Among the solid boundaries and objects, there are a small hole [3], blind holes/crevices [4], rectangular channels [5], convex surfaces [6], a thin gap (parallel plates) [7, 8], rigid spheres [9, 10], a pencil-like electrode [11], ridges and grooves [12], a micro structured riblet [13], edges [14, 15] and corners [16] ([1]).

The investigation of the dynamics of a bubble...
close to the top of a rigid cylinder, both experimental and numerical, is described in this manuscript. The bubble is generated on the symmetry axis of the cylinder. Therefore, three independent parameters describe the geometrical arrangement as shown in Figure 1. $l_p$ — the length of the cylinder (height above a planar, solid boundary), $r_p$ — the radius of the cylinder and $D_{\text{init}}$ — the distance of the bubble to the top of the cylinder at $t = 0$ (i.e. the spot of optical breakdown, hence the plasma spot). The energy of the bubble, given a certain atmospheric pressure, is classified by the maximum radius $R_{\text{max, unbound}}$ the bubble would attain in an unbounded liquid. When the bubble is generated close to an object, the maximum, volume-equivalent radius $R_{\text{max, eq}}$ will differ from the unbounded one, depending on the structure of the object and $D_{\text{init}}$ (see also [17]).

![Figure 1. Sketch of the parameters for classification of bubbles close to a solid cylinder [1].](image)

The dynamics of the bubble scale with the non-dimensionalized parameters

$$D^* = \frac{D_{\text{init}}}{R_{\text{max, unbound}}}, \quad r^* = \frac{r_p}{R_{\text{max, unbound}}},$$

(1)

for $l_p \gg r_p$. With the reference to $R_{\text{max, unbound}}$, the temporal normalization is uniquely defined by the Rayleigh collapse time $t_{\text{RC}}$ given by

$$t_{\text{RC}} = 0.91468 \cdot R_{\text{max, unbound}} \sqrt{\rho_{\infty}/p_{\infty}},$$

(2)

where $\rho_{\infty} = 998.2 \text{ kg/m}^3$ and $p_{\infty} = 101315 \text{ Pa}$. (11).

The case where $l_p = 0$ or $r_p \to \infty$ was and still is heavily studied, it is the case of a bubble close to a flat, rigid boundary. In this case, the bubble will involute and produce a liquid jet towards the solid. Historically, values for $D^* > 0.3$ were investigated, where the jet is called micro-jet and exhibits speeds in the order of 1000 m/s. They are produced by annular inflow with self-impact and by squeezing the liquid into two opposite directions [20]. The findings are in agreement with the simulations by Pishchalnikov et al. [21] and experiments as early as by Benjamin and Ellis [22]. A comparison with very good agreement of the velocities of numerical simulations with experiments of laser-induced bubbles for both the micro-jet and for the fast jet, as well, can be found in the works of Koch [23] and Koch et al. [24]. Later, these results were confirmed by Reuter et al. [25].

Thus, the question arises, whether there are other geometrical configurations where the fast jet is produced. This is indeed the case for the bubble close to the top of a rigid cylinder. The dynamics of the bubble in this case provoke the association with a mushroom shape. The present work investigates the details of the dynamics in the parameter range $0.047 < D^* < 2.009$ and $0.251 < r^* < 0.893$.

2. EXPERIMENTAL METHODS

The observation of the laser-induced bubble in the experiment is described briefly here. For a detailed explanation, the reader is referred to [1].

The bubble is produced in the center of a rectangular cuvette of edge length $1 \text{ cm} \times 5 \text{ cm} \times 4 \text{ cm}$ (width, depth, height), filled with de-ionized water. The laser for bubble seeding is an Nd:YAG Litron nanosecond laser that points onto a photodiode through the site of bubble generation.

For the rigid cylinder, a sewing needle was ground to flat top. The needle radius was measured to be $r_p = 272.8 \mu\text{m}$. Two cameras are applied for observing the bubble, each equipped with a long distance microscope objective (K2 Infinity). For Mega-frames per second recording of the collapse of the bubble the Imacon 468 was used (8 images in total) and for kilo-frames per second recording of the overall dynamics the Photon APS-RX was used. The record trigger for the Imacon Camera has to be known with 1 precision. This was accomplished with a continuous wave Helium-Neon laser that points onto a photodiode through the site of bubble generation.

Backlight illumination was done with a xenon-flash (Mecablitz).

3. BUBBLE MODEL AND NUMERICAL METHODS

The bubble model consists of two phases, one gas phase (air) and one liquid phase (water) that do not exchange mass. Viscosity of both phases is included, while surface tension and gravity are neglected in this case, as well as evaporation or condensation processes. The two phases are considered isentropic, which is valid up to shock waves of $e = 3 \text{ GPa}$ [26, page 40]. Therefore, the energy equation for
the set of momentum equations for the compressible phases can be omitted and can be substituted by two equations of state: the adiabatic gas equation and the Tait-equation

\[
\frac{p}{p_\infty} = \left(\frac{\rho}{\rho_\infty}\right)^\gamma, \quad \text{liquid: } \frac{p + B}{p_\infty + B} = \left(\frac{\rho}{\rho_\infty}\right)^{\gamma T},
\]

where \(\gamma = 1.4\) is the polytropic exponent of air, \(\rho_\infty = 1.204 \text{ kg/m}^3\), \(B = 305 \text{ MPa}\) a constant and \(\gamma_T = 7.15\), the Tait-exponent.

The model is implemented in a finite volume solver running in the open source foam-extend software package for computational fluid dynamics. This solver is maintained and developed since 2013 (for an extended description, including validation, see e.g. [27][28][19][23]).

The governing equations are the Navier-Stokes equation and the continuity equation

\[
\frac{\partial (\rho \mathbf{U})}{\partial t} + \nabla \cdot (\rho \mathbf{U} \otimes \mathbf{U}) = - \nabla p + \nabla \cdot \left[ \mu \left( \nabla \mathbf{U} + (\nabla \mathbf{U})^T \right) - \frac{2}{3} \nabla \cdot (\mathbf{U} \otimes \mathbf{I}) \right],
\]

\[
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0, \quad \frac{\partial \alpha_i}{\partial t} + \nabla \cdot (\alpha_i \rho \mathbf{U}) = 0,
\]

where \(\mathbf{U}\) denotes the velocity, \(\otimes\) the tensorial product, \(\nabla\) the gradient and \(\nabla \cdot\) the divergence, \(\mu\) the dynamic viscosity and \(\mathbf{I}\) the unit tensor. The two phases are distinguished by a phase parameter \(\alpha \in [0, 1]\) such that, e.g., \(\mu = \alpha \mu_l + (1 - \alpha) \mu_g\) with \(\mu_l, \mu_g\) the viscosities of the liquid and the gas respectively. The subscript \(i\) denotes either \(l\) (liquid) or \(g\) (gas), where \(\alpha_l = \alpha\) and \(\alpha_g = 1 - \alpha\).

The computational domain is discretized with the finite volume method and the equations are solved in a segregated manner by the PISO algorithm (pressure implicit with splitting of operators).

### 3.1. Initial data

The calculations have been performed mainly in axial symmetry. Distinct simulations in full 3D have been made for a qualitative comparison, as well. The size of the computational domain for the axisymmetric calculations was chosen to be 52 mm, while the maximum radii in unbounded liquid \(R_{\text{max, unbound}}\) of the bubbles tested ranged from 224 \(\mu\)m to 636 \(\mu\)m. At \(t = 0\) the liquid is at rest and the bubble is compressed to 20 \(\mu\)m in all of the 89 cases studied. The cells of the mesh are oriented in the radial direction, only the core of the mesh is in cartesian orientation. The cylinder with a radius of either 200 \(\mu\)m or 160 \(\mu\)m was cut out of the mesh. The boundary condition at the cylinder is set to no-slip and \(\alpha = 1\) (= liquid). The outer boundary of the mesh is set to be wave transmissive. Details for the mesh are found in [1].

### 3.2. Hardware

The simulations in axial symmetry were done on a dual Xenon Silver 4216 machine with 32 cores and 93.1 GB RAM. Each simulation comprised about 125 000 cells and 30 000 time steps, consuming about 1h15min of computational time for 110 \(\mu\)s.

### 4. RESULTS

Before describing the results of the bubbles on top of a cylinder, the case for \(l_p = 0\) is recapitulated. In Figure 2 the pressure and velocity field of an axisymmetric simulation of a bubble at \(D^* = 0.04\), \(l_p = 0\) are shown for six times shortly before minimum bubble volume in order to elucidate the different jetting mechanism. An annular jet forms on the top of the bubble. The liquid impacts onto itself before the bubble could involute like it would do for \(D^* \geq 0.24\). Within a fraction of a microsecond a small part of the liquid is accelerated to, here, more than 1200 m/s. More information about this phenomenon is found in [18][19][23][24][1], as well as in the CMFF’22 article by C. Lechner.

![Figure 2. Simulation showing the fast-jet mechanism. Reprinted from [23] Fig. 5.1. Left part of the frames: pressure field in bar, right part of the frames: velocity field in m/s.](image-url)
fragmentation into many small gas parts and subsequently the mushroom cap grows and detaches as a projectile.

In order to gain insight into why the mushroom shape of the bubble is formed and whether it is persistent to a wider range of the \( [D^*, r_p] \) parameter space, 89 simulations in axial symmetry have been performed, out of which 68 showed the mushroom shape. 18 frames of one simulation with typical dynamics are shown in Figure 5 with arrows indicating the main flow. The color indicates the magnitude of the velocity of the liquid in m/s. The characteristic values of the bubble are: \( R_{max, unbound} = 472.57 \mu m, D^* = 0.063, r_p = 0.423, t_{rc} = 42.90 \mu s \). Cylinder radius is 200 \( \mu m \). Frames 1–9 show the expansion and the begin of the collapse, while frames 10–18 show the moment of jetting with a fast jet, the bubble minimum volume and rebound with the detaching of the projectile.

During the expansion phase, shown in the first 3 frames the bubble interface crosses the cylinder rim, it swirls around it (frame 2), ejecting liquid droplets (in axial symmetry torus ring drops) into the bubble body. Once passed, these droplets hit the outer bubble wall, inducing surface waves there (dashed circles in frame 3). Due to the boundary layer around the cylinder, the bubble never touches the solid, but “swims” on the boundary layer. (1).

When the bubble starts collapsing, the outer waist is lifted almost parallel to the cylinder. This flow produces the two annular inflows that form a) a neck and b) the extreme curvatures at the mushroom cap rim. As denoted by the red arrows and circles in frame 7, Fig. 5 the flow that forms the mushroom neck has also a component upwards that tapers the cap to a thin gas film. The phenomenon of flow focusing comes into play \([29][19]\), flow focusing generating strongest acceleration where curvatures are highest. An annular jet is formed that runs along the top part of the shrinking mushroom cap, leaving trails of dim remnant gas that form a thin umbrella (see e.g. Fig. 4 right frame). Numerically, this results into a tearing of the interface, leaving areas where \( 0.9 < \alpha < 1 \). In the end, this annular liquid jet impacts in the zenith of the umbrella, producing a fast jet. The fast jet actually is the reason, why the neck will not impact onto itself. It can be seen that the fast jet here reaches values of more than 700 m/s (see dashed rectangle on top of the velocity scale in frame 11). In some cases, it is more than 2000 m/s, as will be shown later. The liquid inflow from the top now, starting from frame 10 on, makes all sideways inflows at the neck negligible, changing the subsequent dynamics to a zipper-like collapse. The neck is tapered from inside rather than from outside flows. In the experiment, only the aforementioned “bottom stand foot” is observed here, because the outside bubble surface has too many wrinkles to see the jet inside. The minimum volume happens from top-down, thus the top gas fragments are already in the rebound phase, when the lower ones collapse and emit shock waves (not seen here – taking place in frame 16, as indicated by the dashed red circle in the frame). Therefore, the upper bubbles are “kicked” and squeezed upwards. Thereby, a layered structure of (torus) bubbles is observed. (1).

Experimental insight into the moment of mushroom bubble jetting can be gained with the Imacon camera. Figure 5 shows such a record of 8 frames at a time during ring jet impact at the top of the mushroom cap. The times denote the delay to the camera trigger. The background of the experimental images was subtracted. The recorded images are compared to a simulation via an overlay with the volume fraction field \( \alpha \) on the left side of each frame (mind that the numerical simulation is represented by a cut through the bubble). The characteristic values for the bubble of the simulation are \( D^* = 0.057 \) and \( r_p = 0.306 \). The frame width for the experiment is \( 766 \mu m \pm 10 \mu m \). The cylinder radius \( r_p \) in the experiment is 272.8 \( \mu m \), in the simulation \( r_p = 200 \mu m \). It is seen that the simulation and the experiment match very well, even the torus-shaped mushroom cap rim is reproduced by the simulation. It is also evident from the simulation that the stem/neck of the bubble is pierced by the fast jet, producing the top-down zipper-like collapse that is also seen in the experiment. For more comparisons, 3D simulations and experimental recordings, the reader again is referred to (1).
Figure 5. General dynamics of the mushroom bubble.
mushroom shape and the fast jet is sketched.

With the figures given in this manuscript, the main line of reasoning concerning the link between the mushroom shape and the fast jet is sketched.

4.1. Parameter study

The 89 simulations were evaluated and distinct quantities were extracted to be plotted into an interpolated heat map with isocurves within the \([D^*, r_p^*]\) parameter space. Two of the graphs from \([1]\) are shown in Figure 7. Each data point represents one simulation. The data points are plotted in their respective colors that represent their values. White data points denote cases, where either the bubble dynamics was different from the mushroom case, the annular jet impact happens later than the neck closure or a standard jet by involution of the bubble wall was observed.

The jet speed (top graph) was calculated by the distance of the spot of the annular jet impact to the top of the cylinder divided by the time the liquid needs to traverse this distance. This speed, however, did not converge yet for any mesh and time resolution (see explanation in \([19, 1]\)). Therefore, the values ranging from 189 m/s to 2164 m/s are given as tentative results. The corresponding water hammer pressures (\(\rho c v_{jet}\)) would range from 0.3 GPa to 3 GPa. The heat map suggests that the faster jets are found for low values of \(r_p^*\) and higher values of \(D^*\).

In the bottom graph the length of the jet is given, measured from the point of formation to the point of impact onto the pillar surface. When the jet length is compared to the cylinder radius, the jet becomes longer for smaller \(r_p^*\) as well (for a fixed \(r_p\)). The jet length varied by less than 10% with grid alterations. It could be an interesting quantity from an experimental point of view, when photographing the jet is planned. (\([1]\)).

5. FURTHER STUDIES

In addition to the material from \([1]\) a glimpse into a probable reason for erosion, first assessed in \([23]\), is given here. For the case of \(l_p = 0\) the pressure signal in the symmetry point below the bubble at the solid wall, gained by an axisymmetric simulation, was compared to the dynamics of the bubble:

It is most likely that the main erosion (for \(l_p = 0\)) happens around \(D^* = 0.1\), where peak values of close to 4 GPa are observed. A first evaluation for the reason of this pressure peak is given in Figure 8 for \(D^* = 0.1\). Shown is the bubble with the pressure field in bar during and after fast jet impact, as well as the aforementioned pressure signal. The fast jet has already impacted onto the solid boundary before the main pressure peak at 111.65 μs. The main peak roots from the focusing of the toroidal shockwave from the collapse of the bubble directly on the solid boundary. From this simulation, it can be said that one single, laser generated bubble of \(R_{max} \approx 500 \mu m\) might be able to erode an alloy when generated at a distance of \(D^* = 0.1\). (\([23]\)). Detailed experimental studies on erosion tests have been performed by \([30, 31]\).

6. SUMMARY

A laser-induced bubble on top of a long cylinder with a radius at maximum volume larger than the radius of the cylinder shows a dynamics very different from a bubble on an extended flat surface. After having embraced the cylinder top upon expansion, upon collapse it develops a mushroom shape with a head, a long stem and a footing. The special fluid flow leading to the mushroom shape could be reproduced in numerical studies by solving the Navier-Stokes equations for a Tait-compressible liquid with OpenFOAM (precisely the foam-extend fork). The
The indication that another cause for erosion might stem from the toroidal shockwave of the bubble collapse has been shown as well for one data point in the parameter subset.

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References


